

2.5 L6-Special Lines in Triangles

Median: A line that joins vertex of a triangle to the midpoint of the opposite side.

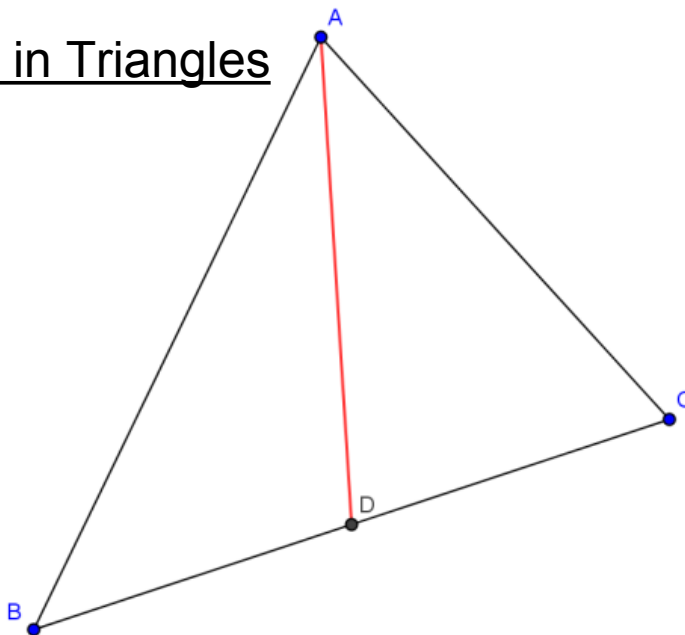
1) Midpoint = M_{BC}

$$2) m_{AD} = \frac{y_D - y_A}{x_D - x_A}$$

3) Sub A or D into

$$y = m_{AD}x + b$$

to solve b



Altitude: A line from a vertex to the opposite side is perpendicular to the opposite side.

1) find slope m_{BC}

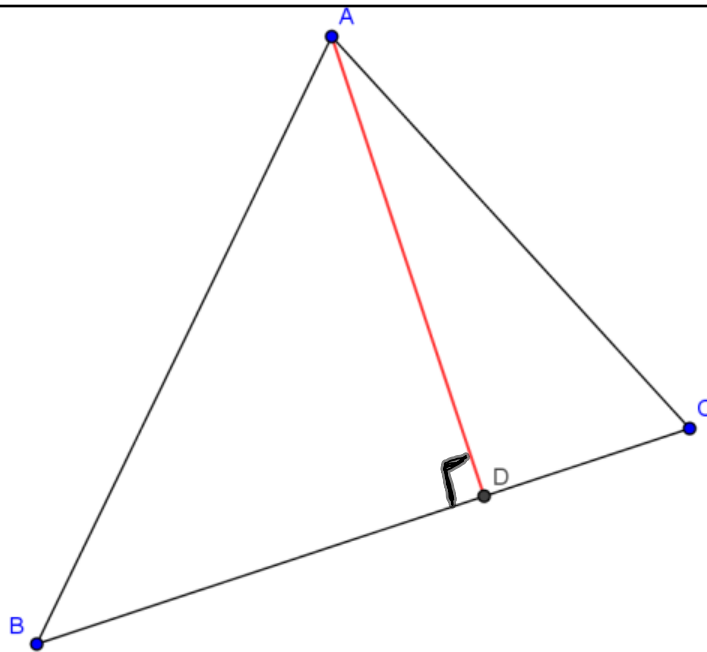
$$2) \text{ state } m_{AD} = -\frac{1}{m_{BC}}$$

$$3) y = m_{AD}x + b$$

4) sub point A into

$$y = m_{AD}x + b$$

to solve b



Perpendicular Bisect

A perpendicular line through the midpoint of a line segment.

1) Midpoint = M_{BC}

2) find slope m_{BC}

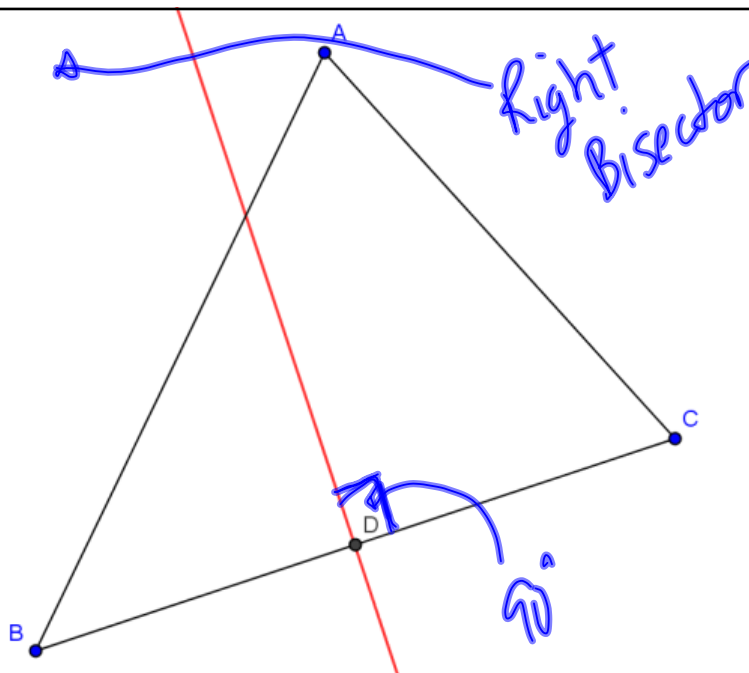
3) state $m_{\perp} = -\frac{1}{m_{BC}}$

4) $y = m_{\perp}x + b$

3) Sub D into

$$y = m_{\perp}x + b$$

to solve b

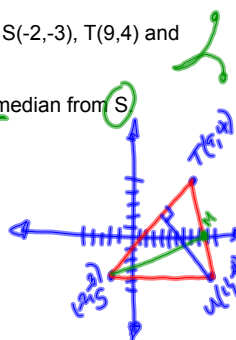
L6-Special Lines in Triangles

Important: make a sketch so you don't get confused.

Ex. 1 Triangle STU has vertices at S(-2,-3), T(9,4) and U(11,-4).

a. Find the equation of the median from S

$$\begin{aligned} M_{TU} &= \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right) \\ &= \left(\frac{9 + 11}{2}, \frac{4 + (-4)}{2} \right) \\ &= (10, 0) \end{aligned}$$



$$\begin{aligned} m_{MS} &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{0 - (-3)}{10 - (-2)} \\ &= \frac{3}{12} \\ &= \frac{1}{4} \end{aligned}$$

$$\begin{aligned} y &= \frac{1}{4}x + b \\ 0 &= \frac{1}{4}(10) + b \\ 0 &= \frac{10}{4} + b \\ b &= -\frac{5}{2} \end{aligned}$$

∴ the equation of the median is $y = \frac{1}{4}x - \frac{5}{2}$

Ex.1 continues...

Triangle STU has vertices at S(-2,-3), T(9,4) and U(11, -4).

b. Find the equation of the altitude from U.

$$\begin{aligned}
 m_{TS} &= \frac{y_2 - y_1}{x_2 - x_1} & m_{\perp} &= -\frac{11}{7} \\
 &= \frac{4 - (-3)}{9 - (-2)} & y &= -\frac{11}{7}x + b \\
 &= \frac{7}{11} & -4 &= -\frac{11}{7}(11) + b \\
 & & -4 &= -\frac{121}{7} + b \\
 & & -4 + \frac{121}{7} &= b \\
 & & -\frac{28}{7} + \frac{121}{7} &= b \\
 & & \frac{93}{7} &= b \\
 & & b &= \frac{93}{7}
 \end{aligned}$$

Sub $u(11, -4)$ do
solve b

\therefore the equation of the altitude is
 $y = -\frac{11}{7}x + \frac{93}{7}$

Ex.1 continues...

Triangle STU has vertices at S(-2,-3), T(9,4) and U(11, -4).

c. Find the equation of the perpendicular bisector of side TU.

$$\begin{aligned}
 M_{TU} &= (10, 0) & m_{\perp} &= \frac{1}{4} \\
 m_{TU} &= \frac{y_2 - y_1}{x_2 - x_1} & y &= \frac{1}{4}x + b \\
 &= -4 & 0 &= \frac{1}{4}(b) + b \\
 & & 0 &= \frac{10}{4} + b \\
 & & -\frac{10}{4} &= b \\
 & & b &= -\frac{5}{2}
 \end{aligned}$$

Sub $(10, 0)$ do
solve b

\therefore the right bisector is
 $y = \frac{1}{4}x - \frac{5}{2}$

Assigned Work:

Triangle ABC has vertices A(3, 4), B(-5, 2) and C(1, -4).
Find the equation for the altitude from A to BC.

p.79 #12

p.80 #13

p.102 #4

p.110 #13